

Grade 8

Grade 8: Content and Reporting Targets

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

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Term 1 – Content Targets	Term 2 – Content Targets	Term 3 – Content Targets			
Number Sense and Numeration*	Number Sense and Numeration*	Number Sense and Numeration*			
• integers	• fractions	 proportional reasoning 			
 order of operations 	• percents	• rates			
 powers and square roots 	Measurement*	Measurement			
 representations of numbers 	• surface area and volume of cylinders	relationships among units			
Measurement*	Geometry and Spatial Sense*	Geometry and Spatial Sense*			
circle measurement relationships	• properties of lines, angles, triangles, and	• similar figures			
Geometry and Spatial Sense	quadrilaterals	Pythagorean Relationship			
• construction of a circle	Patterning and Algebra	properties of polyhedra			
Patterning and Algebra*	• use patterns to develop measurement	• transformations on the plane			
algebraic expressions	formulas	Patterning and Algebra*			
multiple representations of patterns	Data Management and Probability*	• solve and verify linear equations			
• writing nth terms	experimental vs. theoretical probability	Data Management and Probability*			
Data Management and Probability	complementary events	design and carry out an experiment			
display and interpret data found in					
patterns	D # 1				
	Rationale				
Connections between:	Connections between:	Connections between:			
- integer size/area of squares	-unit rate problems/Term 1 algebra	- fractions/ratios/unit rates/percent			
- integer sign/colour of integer tile	- geometric properties/data management	- natural/whole/integer/fractional/			
- integers/order of operations	- angle properties/Term 1 algebra	rational/irrational sets of numbers			
-powers and square roots/inverse	-theoretical and experimental probability/	(combining natural, whole, integer, and			
operations	effect of sample size	fractional numbers)			
- constructing circles/discovering	- fractions/percents/decimals	– solving equations/Integers and fractions			
relationships between circle	– volume of triangular prism and Grades 6	-solving equations/unit rates and			
measurements	and 7 concept of Volume = area of	proportions			
-algebraic expressions/generalizations of	base × height	- connecting properties of triangles/similar			
patterns	- circles/volume of a cylinder	triangles and Pythagorean relationship			
- different algebraic representations of a	- connecting properties of triangles/data	-data from Term 1 and 2 investigations/			
pattern/the values generated by	management	associated concepts/designing an			
substitution into those representations	Leading to:	experiment			
- statements/algebraic expressions	-connecting unit rates with percents and	Leading to:			
Leading to:	fractions (Term 3)	- combining rational numbers (Grade 9)/			
- connection between powers/ measurement	-connecting fractions and percents to rates,	irrational numbers (Grade 11 University			
units (Term 3)	ratios, and proportions (Term 3)	destination)			
-powers and square roots/applying inverse	- combining perimeter/area of irregular	- solving equations requiring collection of			
operations to solve equations involving	shapes with circles (Grade 9)	like terms (Grade 9)			
the Pythagorean relationship (Grade 9)	- connecting volume of cylinder to volume	- solving equations involving the			
-combining rational and irrational numbers	of any prism (Grade 9)	Pythagorean relationship (Grade 9)			
(Grade 11)	- extending probability/statistics	- extending transformations of 2-D shapes			
- connecting order of operations with	(Grade 12)	to transformations of functions (Grades			
integers to order of operations with	- connecting properties of triangles/similar	10, 11)			
fractions	triangles and Pythagorean relationship	- extending data management techniques			
-applications of algebraic expressions to	(Term 3)	(Grade 12)			
unknowns in equations (Term 3)	-relating properties of 2-D figures to 3-D				
-using both theoretical and experimental	figures (Term 3)				
means of finding patterns (Terms 2)	- extending properties of lines, angles,				
	triangles and quadrilaterals (Grade 9)				

^{*} Strands for reporting purposes

Grade 8: Number Sense and Numeration

Term 1 Term 2 Term 3

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

Integers

8m16 – solve multi-step problems arising from real-life contexts and involving whole numbers and decimals, using a variety of tools (e.g., graphs, calculators) and strategies (e.g., estimation, algorithms);

8m18 – use estimation when solving problems involving operations with... integers ... to help judge the reasonableness of a solution; 8m21 – represent the multiplication and division of integers, using a variety of tools (e.g., if black counters represent positive amounts and red counters represent negative amounts, you can model $3 \times (-2)$ as three groups of two red counters):

8m22 – solve problems involving operations with integers, using a variety of tools (e.g., two-colour counters, virtual manipulatives, number lines).

Order of Operations

8m23 – evaluate expressions that involve integers, including expressions that contain brackets and exponents, using order of operations.

Powers and Square Roots

8m11 – express repeated multiplication using exponential notation (e.g., $2 \times 2 \times 2 \times 2 = 2^4$); 8m24 – multiply and divide decimal numbers by various powers of ten (e.g., "To convert 230 000 cm₃ to cubic metres, I calculated in my head $23\ 0000 \div 10^6$ to get $0.23\ m^3$.");

8m25 – estimate, and verify using a calculator, the positive square roots of whole numbers, and distinguish between whole numbers that have whole-number square roots (i.e., perfect square numbers) and those that do not.

Representations of Numbers

8m12 – represent whole numbers in expanded form using powers of ten (e.g., $347 = 3 \times 10^2 + 4 \times 10^1 + 7$);

8m13 – represent, compare, and order rational numbers (i.e., positive and negative fractions and decimals to thousandths).

Fractions

8m13 – represent, compare, and order rational numbers (i.e., positive and negative fractions and decimals to thousandths);

8m15 – determine common factors and common multiples using the prime factorization of numbers (e.g., the prime factorization of 12 is $2 \times 2 \times 3$; the prime factorization of 18 is $2 \times 3 \times 3$; the greatest common factor of 12 and 18 is 2×3 or 6; the least common multiple of 12 and 18 is $2 \times 2 \times 3 \times 3$ or 36).

8m18 – use estimation when solving problems involving operations with... and fractions to help judge the reasonableness of a solution; 8m19 – represent the multiplication and division of fractions, using a variety of tools and strategies (e.g., use an area model to represent $\frac{1}{4}$

multiplied by $\frac{1}{3}$);

8m20 – solve problems involving addition, subtraction, multiplication, and division with simple fractions.

Percents

8m14 – translate between equivalent forms of a number, i.e., decimals, fractions, percents) (e.g., $\frac{3}{4} = 0.75$);

8m16 – solve multi-step problems arising from real-life contexts and involving...and decimals, using a variety of tools and strategies (e.g., estimation, algorithms);

8m17 – solve problems involving percents expressed to one decimal place (e.g., 12.5%) and whole-number percents greater than 100 (e.g., 115%).

8m18 – use estimation when solving problems involving operations with... decimals, percents...to help judge the reasonableness of a solution:

8m28 – solve problems involving percent that arise from real-life contexts (e.g., discount, sales tax, simple interest);

8m29 – solve problems involving rates.

Proportional Reasoning

8m18 – use estimation when solving problems involving operations with whole numbers, decimals, percents, integers, and fractions, to help judge the reasonableness of a solution; 8m23 – evaluate expressions that involve integers, including expressions that contain brackets and exponents, using order of operations;

8m26 – identify and describe real-life situations involving two quantities that are directly proportional (e.g., the number of servings and the quantities in a recipe, mass and volume of a substance, circumference and diameter of a circle);

8m27 – solve problems involving proportions, using concrete materials, drawings, and variables.

Rates

8m29 - solve problems involving rates.

Grade 8: Measurement Term 1 Term 2 Term 3

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

Circle Measurement Relationships

8m34 – measure the circumference, radius, and diameter of circular objects, using concrete materials;

8m35 – determine, through investigation using a variety of tools (e.g., cans and string, dynamic geometry software) and strategies, the relationships for calculating the circumference and the area of a circle, and generalize to develop the formulas,

[i.e., Circumference of a circle = $\pi \times$ diameter; Area of a circle = $\pi \times$ (radius)²];

8m36 – solve problems involving the estimation and calculation of the circumference and the area of a circle.

Surface Area and Volume of Cylinders

8m32 – research, describe, and report on applications of volume and capacity measurement (e.g., cooking, closet space, aquarium size);
8m33 – solve problems that require conversions involving metric units of area, volume, and capacity (i.e., square centimetres and square metres; cubic centimetres and cubic metres; millilitres and cubic centimetres);
8m37 – determine, through investigation using a variety of tools and strategies (e.g., generalizing from the volume relationship for right prisms, and verifying using the capacity of thin-walled cylindrical containers), the relationship between the area of the base and height and the volume of

the area of the base and height and the volume of a cylinder, and generalize to develop the formula (i.e., Volume = area of base × height); 8m38 – determine, through investigation using concrete materials, the surface area of a cylinder; 8m39 – solve problems involving the surface area and the volume of cylinders, using a variety of strategies.

Relationships Among Units

8m33 – solve problems that require conversions involving metric units of area, volume, and capacity (i.e., square centimetres and square metres; cubic centimetres and cubic metres; millilitres and cubic centimetres).

Grade 8: Geometry and Spatial Sense

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

Selecting Tools and Computational Strategies, Connecting, Representing, Communicating						
Term 1	Term 2	Term 3				
Construction of a Circle 8m44 – construct a circle, given its centre and radius, or its centre and a point on the circle, or three points on the circle; 8m45 – investigate and describe applications of geometric properties (e.g., properties ofand circles) in the real world.	Properties of Lines, Angles, Triangles, and Quadrilaterals 8m43 – sort and classify quadrilaterals by geometric properties, including those based on diagonals, through investigation using a variety of tools (e.g., concrete materials, dynamic geometry software); 8m45 – investigate and describe applications of geometric properties (e.g., properties of triangles, quadrilaterals) in the real world; 8m47 – determine, through investigation using a variety of tools (e.g., dynamic geometry software, concrete materials, protractor) and strategies (e.g., paper folding), the angle relationships for intersecting lines and for parallel lines and triangle; 8m48 – solve angle-relationship problems involving triangles (e.g., finding interior angles or complementary angles), intersecting lines (e.g., finding supplementary angles or opposite angles), and parallel lines and transversals (e.g., finding alternate angles or corresponding angles).	Similar Figures 8m46 – determine, through investigation using a variety of tools (e.g., dynamic geometry software, concrete materials, geoboard), relationships among area, perimeter, corresponding side lengths, and corresponding angles of similar shapes. Pythagorean Relationship 8m49 – determine the Pythagorean relationship, through investigation using a variety of tools (e.g., dynamic geometry software, paper and scissors, geoboard) and strategies; 8m50 – solve problems involving right triangles geometrically, using the Pythagorean relationship. Properties of Polyhedra 8m51 – determine, through investigation using concrete materials, the relationship between the numbers of faces, edges, and vertices of a polyhedron (i.e., number of faces + number of vertices = number of edges + 2). Transformations on the Plane 8m52 – graph the image of a point, or set of points, on the Cartesian coordinate plane after applying a transformation to the original point(s) (i.e., translation; reflection in the x-axis, the y-axis, or the angle bisector of the axes that passes through the first and third quadrants; rotation of 90°, 180°, or 270° about the origin); 8m53 – identify, through investigation, real-world movements that are translations, reflections, and rotations.				

Grade 8: Patterning and Algebra

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

Term 1	Term 2	Term 3
Algebraic Expressions 8m56 – represent, through investigation with concrete materials, the general term of a linear pattern, using one or more algebraic expressions (e.g., "Using toothpicks, I noticed that 1 square needs 4 toothpicks, 2 connected squares need 7 toothpicks, and 3 connected squares need 10 toothpicks. I think that for n connected squares I will need $4 + 3(n - 1)$ toothpicks"); 8m59 – describe different ways in which algebra can be used in real-life situations; 8m61 – translate statements describing mathematical relationships into algebraic expressions; 8m62 – evaluate algebraic expressions with up to three terms, by substituting fractions, decimals, and integers for the variables (e.g., evaluate $3x + 4y = 2z$, where $x = \frac{1}{2}$, $y = 0.6$, and $z = -1$). Multiple Representations of Patterns 8m57 – represent linear patterns graphically (i.e., make a table of values that shows the term number and the term, and plot the coordinates on a graph), using a variety of tools (e.g., graph paper, calculators, dynamic statistical software). Writing the n th Term 8m58 – determine a term, given its term number, in a linear pattern that is represented by a graph or an algebraic equation. 8m60 – model linear relationships using tables of values, graphs, and equations (e.g., the sequence 2, 3, 4, 5, 6can be represented by the equation $t = n + 1$, where n represents the term number and t represents the term), through investigation using a variety of tools; 8m63 – make connections between solving equations and determining the term number in a pattern, using the general term (e.g., for the pattern with the general term $2n + 1$, solving the equation $2n + 1 = 17$ tells you the term number when the term is 17).	Use Patterns to Develop Measurement Formulas 8m61 – translate statements describing mathematical relationships into algebraic expressions and equations; 8m62 – evaluate algebraic expressions with up to three terms, by substituting fractions, decimals, and integers for the variables (e.g., evaluate $3x + 4y = 2z$, where $x = \frac{1}{2}$, $y = 0.6$, and $z = -1$).	Solve and Verify Linear Equations 8m56 – represent, through investigation with concrete materials, the general term of a linear pattern, using one or more algebraic expressions (e.g., "Using toothpicks, I noticed that 1 square needs 4 toothpicks, 2 connected squares need 7 toothpicks, and 3 connected squares need 10 toothpicks. I think that for n connected squares I will need $4 + 3(n - 1)$ toothpicks"); 8m59 – describe different ways in which algebra can be used in real-life situations; 8m61 – translate statements describing mathematical relationships into algebraic expressions and equations (e.g., for a collection of triangles, the total number of sides is equal to three times the number of triangles or $s = 3n$); 8m62 – evaluate algebraic expressions with up to three terms, by substituting fractions, decimals, and integers for the variables (e.g., evaluate $3x + 4y = 2z$, where $x = \frac{1}{2}$, $y = 0.6$, and $z = -1$); 8m63 – make connections between solving equations and determining the term number in a pattern, using the general term (e.g., for the pattern with the general term $2n + 1$, solving the equation $2n + 1 = 17$ tells you the term number when the term is 17); 8m64 – solve and verify linear equations involving a one-variable term and having solutions that are integers, by using inspection, guess and check, and a "balance" model.

Grade 8: Data Management and Probability

Mathematical Process Expectations across all strands and terms: Problem Solving, Reasoning and Proving, Reflecting, Selecting Tools and Computational Strategies, Connecting, Representing, Communicating

Term 1 Term 2 Term 3 Display and Interpret Data Found in **Experimental vs. Theoretical Probability Design and Carry Out an Investigation Problems** 8m70 - collect and organize categorical, discrete, 8m68 – collect data by conducting a survey or an or continuous primary data and secondary data 8m68 – collect data by conducting a survey or an experiment to do with themselves, their experiment to do with themselves, their (e.g., electronic data from websites such as E-Stat environment, issues in their school or community, or Census At Schools), and display the data in environment, issues in their school or community, or content from another subject, and record or content from another subject, and record charts, tables, and graphs (including histograms observations or measurements; observations or measurements: and scatter plots) that have appropriate titles, 8m69 – organize into intervals a set of data that is 8m70 - collect and organize... continuous labels (e.g., appropriate units marked on the spread over a broad range (e.g., the age of primary data ...and display the data in charts, axes), and scales (e.g., with appropriate respondents to a survey may range over 80 years tables, and graphs...; increments) that suit the range and distribution of and may be organized into ten-year intervals); the data, using a variety of tools (e.g., graph 8m73 – read, interpret, and draw conclusions 8m70 – collect and organize categorical, discrete, from primary data (e.g., survey results, paper, spreadsheets, dynamic statistical software) or continuous primary data and secondary data (e.g., electronic data from websites such as E-Stat 8m80 – compare, through investigation, the measurements, observations)...presented in charts, tables, and graphs; theoretical probability of an event (i.e., the ratio or Census At Schools), and display the data in 8m74 – determine, through investigation, the of the number of ways a favourable outcome can charts, tables, and graphs (including histograms occur compared to the total number of possible appropriate measure of central tendency; and scatter plots) that have appropriate titles, outcomes) with experimental probability, and labels (e.g., appropriate units marked on the 8m78 - make inferences and convincing arguments that are based on the analysis of charts. explain why they might differ; axes), and scales (e.g., with appropriate tables, and graphs; 8m81 – determine, through investigation, the increments) that suit the range and distribution of 8m79 - compare two attributes or characteristics, tendency of experimental probability to approach the data, using a variety of tools (e.g., graph paper, spreadsheets, dynamic statistical software); using a variety of data management tools and theoretical probability as the number of trials in strategies (i.e., pose a relevant question, then an experiment increases, using class-generated 8m71 – select an appropriate type of graph to design an experiment or survey, collect and data and technology-based simulation models; represent a set of data, graph the data using analyse the data, and draw conclusions). technology, and justify the choice of graph (i.e., **Complementary Events** from types of graphs already studied, including 8m82 – identify the complementary event for a histograms and scatter plots); given event, and calculate the theoretical 8m72 – explain the relationship between a probability that a given event will not occur. census, a representative sample, sample size, and a population (e.g., "I think that in most cases a larger sample size will be more representative of the entire population."); 8m73 – read, interpret, and draw conclusions from primary data (e.g., survey results, measurements, observations) and from secondary data (e.g., election data or temperature data from the newspaper, data from the Internet about lifestyles), presented in charts, tables, and graphs (including frequency tables with intervals, histograms, and scatter plots); 8m75 – demonstrate an understanding of the appropriate uses of bar graphs and histograms by comparing their characteristics; 8m76 – compare two attributes or characteristics (e.g., height versus arm span), using a scatter plot, and determine whether or not the scatter plot suggests a relationship; 8m77 – identify and describe trends, based on the rate of change of data from tables and graphs, using informal language (e.g., "The steep line going upward on this graph represents rapid growth. The steep line going downward on this other graph represents rapid decline."); 8m78 – make inferences and convincing arguments that are based on the analysis of charts, tables, and graphs; 8m79 – compare two attributes or characteristics, using a variety of data management tools and strategies (i.e., pose a relevant question, then design an experiment or survey, collect and analyse the data, and draw conclusions).

Grade 8 Year Outline – Planning Tool

- P Number of planned lessons (including instruction, diagnostic and formative assessments, summative assessments other than included performance tasks)
- J Number of Jazz days
- Total number of days

Term	Unit	Cluster of Curriculum Expectation	Overall Expectations	P	J	Т
	0	Introductory Unit: Developing Social Skills Within the Context of Problem Solving	 8m1 develop, select, apply, and compare a variety of problem-solving strategies as they pose and solve problems and conduct investigations, to help deepen their mathematical understanding 8m3 demonstrate that they are reflecting on and monitoring their thinking to help clarify their understanding as they complete an investigation or solve a problem (e.g., by assessing the effectiveness of strategies and processes used, by proposing alternative approaches, 	6 (6 included)	4	10
			by judging the reasonableness of results, by verifying solutions) 8m7 communicate mathematical thinking orally, visually, and in writing, using mathematical vocabulary and a variety of appropriate representations, and observing mathematical conventions			
1	1	Integers and Algebraic Expressions	8m9 solve problems involving whole numbers, decimal numbers, fractions, and integers, using a variety of computational strategies	12 (12 included)	4	16
	2	Representing Patterns in Multiple Ways	8m54 represent linear growing patterns (where the terms are whole numbers) using graphs, algebraic expressions, and equations 8m55 model linear relationships graphically, and algebraically and solve and verify algebraic equations, using a variety of strategies, including inspection, guess and check, and using a "balance" model.	7 (7 included)	4	11
	3	From Powers to Circles	8m8 represent, compare, and order equivalent representations of numbers, including those involving positive exponents 8m31 determine the relationships among units and measurable attributes including the area of a circle and the volume of a cylinder 8m40 demonstrate an understanding of the geometric properties of quadrilaterals circles and the applications of these geometric properties in the real world	11 (10 included)	7	18
		Sub-totals		36	19	55
	4	Lines, Angles, Triangles and Quadrilaterals	8m40 demonstrate an understanding of the geometric properties of quadrilaterals and circles and the applications of geometric properties in the real world 8m41 develop geometric relationships involving lines, triangles, and polyhedra, and solve problems involving lines and triangles	13 (11 included)	3	16
2	5	Fractions and Percents	 8m8 represent, compare, and order equivalent representations of numbers, including those involving positive exponents 8m9 solve problems involving whole numbers, decimal numbers, and fractions and integers, using a variety of computational strategies 8m10 solve problems by using proportional reasoning in a variety of meaningful contexts 	17 (17 included)	7	24

Term	Unit	Cluster of Curriculum Expectation	Overall Expectations	Р	J	Т
	6	Probability	8m67 use probability models to make predictions about real-life events	7 (7 included)	3	10
2	7	Surface Area and Volume of Cylinders	 8m30 research, describe, and report on applications of volume and capacity measurement 8m31 determine the relationships among units and measurable attributes, including the area of a circle and the volume of a cylinder 	7 (6 included)	3	10
		Sub-totals		44	16	60
	8	Proportional Reasoning	8m10 solve problems by using proportional reasoning in a variety of meaningful contexts	8 (8 included)	4	12
	9	Similar Figures	8m40 demonstrate an understanding of the geometric properties of quadrilaterals and circles and the applications of geometric properties in the real world 8m41 develop geometric relationships involving lines, triangles and polyhedra, and solve problems involving lines and triangles	6 (0 included)	2	8
3	10	Visualizing Geometric Relationships	8m40 demonstrate an understanding of the geometric properties of quadrilaterals and circles and the applications of geometric properties in the real world 8m41 develop geometric relationships involving lines, circles and triangles, and polyhedra, solve problems involving lines and triangles 8m42 represent transformations using the Cartesian coordinate plane, and make connections between transformations and the real world	14 (14 included)	6	20
	11	Design and Carry Out an Experiment	8m65 collect and organize categorical, discrete, or continuous primary data and secondary data and display the data using charts and graphs, including frequency tables with intervals, histograms, and scatter plots 8m66 apply a variety of data management tools and strategies to make convincing arguments about data 8m67 use probability models to make predictions about real-life events	11 (11 included)	3	14
	12	Solving Equations	8m55 model linear relationships graphically and algebraically and solve and verify algebraic equations, using a variety of strategies, including inspection, guess and check, and using a "balance" model	7 (0 included)	4	11
		Sub-totals		46	19	65
Total Days				126	54	180

The number of planned lessons represents the lessons that could be planned ahead based on the range of student readiness, interests, and learning profiles that can be expected in a class. The extra time available for "instructional jazz" can be taken a few minutes at a time within a pre-planned lesson, or taken a whole class at a time, as informed by teachers' observations of student needs.

The reference numbers are intended to indicate which lessons are planned to precede and follow each other. Actual day numbers for particular lessons and separations between terms will need to be adjusted by teachers.